

- today : - learning to search
- SeaRNN
  - SPENS

Learning to search (L2S)

SEARN Hal Daume's PhD thesis

$h_w: X \rightarrow Y$

$h_w(x) = \underset{y \in Y}{\text{argmax}} s(x, y; w)$  ] parametrized search procedure

today: special case of SEARN: learning to do greedy search

split  $y$  in ordered list of decisions

$(y_1, y_2, \dots, y_T)$

learn a classifier  $\pi_w(\text{feature}(\hat{y}_1, \hat{y}_2, \dots, \hat{y}_{t-1}; x)) = \hat{y}_t$   
 ↑ classifier "decoding policy"

L2S framework

from  $(x^{(i)}, y^{(i)})_{i=1}^n$  and  $l(\cdot, \cdot)$

learn a good classifier/policy  $\pi_w$  s.t.  $\hat{y}_t = \pi_w(\mathcal{L}(\hat{y}_{1:t-1}; x))$   
 $h_w(x) \triangleq (\hat{y}_1, \dots, \hat{y}_T)$  "greedy decoder"  
 s.t.  $l(y^{(i)}, h_w(x^{(i)}))$  is small

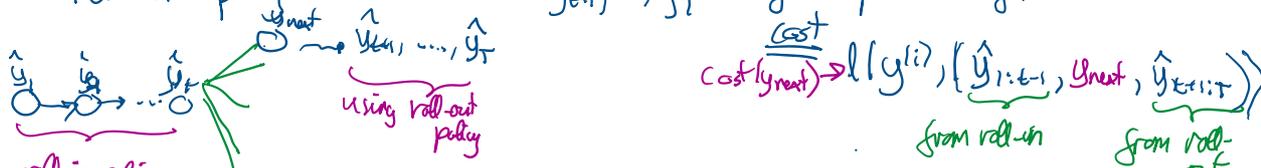
⊗ central idea: "reduction" where reduces structured prediction problem to problem of cost sensitive classification learning of  $\pi_w$

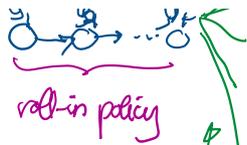
method: generate training data for classifier  $\pi_w$

$(\hat{y}_{\text{context}}^{(j)}, x^{(j)}, \text{cost}(y_{\text{next}}))$   
 ↑ cost function of  $y_{\text{next}}$   
 prefer sequence to make next prediction

"roll in" policy → determines how  $\hat{y}_{1:t-1}$  context

"roll out" policy → " " "  $y_{t+1}, \dots, y_T$  "forget completion" to get





using roll-out policy

loss  $(y_{next}) \dots (y_{1:t-1}, y_{next}, y_{t:t+T})$   
 from roll-in      from roll-out

choices of  $y_{next}$  for  $\pi_w$

then  
 idea is to define surrogate loss for  $\pi_w$  as function of  $cost(y_{next})$

ex of roll-out:

"reference policy", ideally,  $\pi_{ref} (y_{1:t-1}, y_{next})$

$$= \underset{y_{completion}}{\text{argmin}} \ell(y_{li}, (y_{1:t-1}, y_{next}, y_{completion}))$$

intractable (NP hard) in general

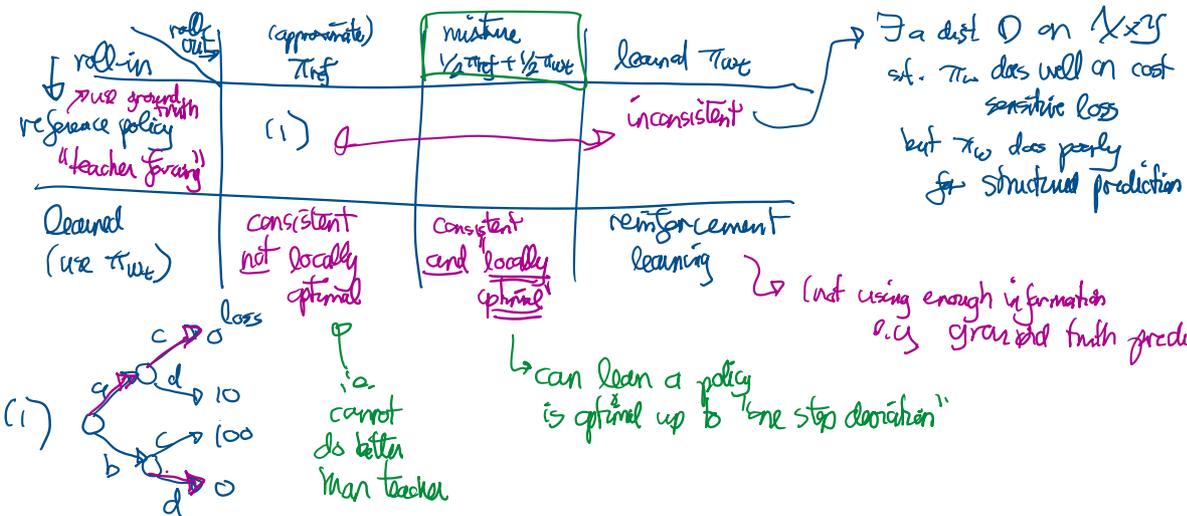
in practice: use heuristic to approximate  $\pi_{ref}$

but sometimes, can compute exactly

e.g.  $\pi_{ref}$  for Hamming loss: is just copying ground truth

LOLS  $\rightarrow$  "locally optimal learning to search"

ICML 2015 "LDS better than your teacher"



example of approximate  $\pi_{ref}$ :  $\ell$  is bleu score (in machine translation)

consider all possible suffixes of ground truth and pick best bleu score

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PEARL: apply LDS to RNN training

[Leland et al., ICML 2018] is  $\pi_w(y_{1:t-1}, x) \rightarrow$  RNN cell

$p(y_{next} | y_{1:t-1}, x)$  of a (decoder) RNN

if you use  $-\log p(\hat{y}_{target} | y_{1:t-1}, x)$  as a cost surrogate

if you use  $-\log p(\hat{y}_{\text{target}} | y_{1:t-1}, x)$  as a cost surrogate

and  $\hat{y}_{\text{target}} = \text{ground truth}$

then LAS with learned roll-in is standard MLE

⊗ cost-sensitive surrogate losses choices

a) structured SVM :  $\max_y [\underbrace{\Delta(y')} + s(y')] - s(y_{\text{target}})$

$\Delta \triangleq c(y') - c(y_{\text{target}})$   
 $y_{\text{target}} \triangleq \underset{y'}{\text{argmin}} c(y')$

b) "target log-loss" :  $-\log p_w(y_{\text{target}} | y_{1:t-1}, x)$

↳ differences with MLE:

- address exposure bias using learned roll-in
- make use of structured loss  $\Delta(\cdot)$  to predict  $y_{\text{target}}$  v.s. ground truth in MLE

Structured prediction energy networks (SPENs)

ICML 2016

$E(x, y; w) \quad (-s(x, y; w))$

• relax  $y \in \{0, 1\}^T \rightarrow [0, 1]^T$

$hw(x) =$  a few steps of projected G.D. on  $E(x, y; w)$  (approximate prediction procedure)  
 w.r.t. to  $y$   
 + rounding

2016 paper:

SSVM loss  $\rightarrow$  "subgradient" method on  $w$

large loss  $\underset{y^*(w)}{\text{argmax}}_{y \in [0, 1]^T} (l(y^{(i)}, \bar{y}) - E(x^{(i)}, \bar{y}; w) + E(x^{(i)}, y^{(i)}; w))$   
 requires estimation through PGD

approximate "subgradient" is  $-\nabla_w E(x^{(i)}, y^*(w); w) + \nabla_w E(x^{(i)}, y^{(i)}; w)$

because  $\bar{y}^*$  is approximate max

e.g. see Clarke subdifferential for generalization on non-convex fct.

2017 paper: end-to-end training

$hw(x) = y_0 - \sum_{t=1}^T \eta_t \frac{d}{dy} E(x, y_t; w)$  "unrolled optimization"  
 recursively defined

$$y_0 \leftarrow y_0 - \eta \frac{d}{dy} E(x, y, \omega)$$

numerical optimization -

$$y_1 = y_0 - \eta_1 \frac{d}{dy} E(x, y_0, \omega)$$

$$y_2 = y_1 - \eta_2 \frac{d}{dy} E(x, y_1, \omega) \text{ etc...}$$